Please write clearly in block capitals.

Centre number |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |

Candidate number


Surname
Forename(s)
Candidate signature

## GCSE

## Mathematics

Higher


## Summer 2019

Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- a calculator
- mathematical instruments.



## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to the answer book.


## Advice

- In all calculations, show clearly how you work out your answer.

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| 3 |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| $18-19$ |  |
| $20-21$ |  |
| $22-23$ |  |
| $24-25$ |  |
| $26-27$ |  |
| TOTAL |  |

## Practice Paper Overview



1 Work out

$$
\binom{-5}{4}-\binom{-7}{4}
$$

Circle your answer.

$$
\binom{-13}{4} \quad\binom{-13}{0} \quad\binom{2}{0} \quad\binom{2}{4} \quad\binom{13}{0}
$$

$2 \quad P$ is $(6,7)$ and $Q$ is $(-4,1)$
Circle the midpoint of $P Q$.
$(5,4)$
$(1,4)$
$(-2,6)$

3 Circle the equation of a straight line which is parallel to

$$
5 y+10 x-25=0
$$

$$
y=2 x+9 \quad 2 x=20-y \quad 2 y=12-x \quad y=\frac{x}{2}-10
$$

4 The bearing of $B$ from $A$ is $075^{\circ}$.


Circle the bearing of $A$ from $B$.
$105^{\circ}$
$075^{\circ}$
$255^{\circ}$

5 Solve the inequality

$$
7-\frac{x}{2} \leq 3
$$

## Answer

$\qquad$

6 Sally won a race with a time of 89.2 seconds.
This time, $t$, is to the nearest tenth of a second.
Complete the error interval due to rounding.
[2 marks]
$\qquad$
$\qquad$
$\leq t<$
$7 y$ is directly proportional to the square of $x$.

| $x$ | 6 | $a$ |
| :---: | :---: | :---: |
| $y$ | 9 | 16 |

Work out the value of $a$.

$$
a=
$$

$\qquad$

8 Here is some information about 40 buses arriving back at the bus depot.

| Number of <br> minutes late, $\mathbf{t}$ | Number of <br> buses | Midpoint |  |
| :---: | :---: | :---: | :--- |
| $0 \leq t<5$ | 8 |  |  |
| $5 \leq t<15$ | 11 |  |  |
| $15 \leq t<20$ | 15 |  |  |
| $20 \leq t<30$ | 6 |  |  |
| $t \geq 30$ | 0 |  |  |

8 (a) Work out an estimate of the mean number of minutes late.

Answer $\qquad$

8 (b) The depot manager scrutinises the information in more detail.

| Number of <br> minutes late, $\mathbf{t}$ | Number of <br> buses |
| :---: | :---: |
| $0 \leq t<5$ | 8 |
| $5 \leq t<10$ | 0 |
| $10 \leq t<15$ | 11 |
| $15 \leq t<20$ | 15 |
| $20 \leq t<25$ | 1 |
| $25 \leq t<30$ | 5 |
| $t \geq 30$ | 0 |

She works out an estimate of the mean using this information.
How does her estimate compare with the answer to part (a)? Tick one box.


Same as part (a)


Higher than part (a)


Not possible to tell

## 9 Expand and simplify

$$
(2 x+3)^{2}(x-1)
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

10 The ratio of $x: y=3: 2$
10 (a) Circle the correct statement.

$$
y \text { is } \frac{3}{5} \text { of } x \quad y \text { is } \frac{2}{5} \text { of } x \quad y \text { is } \frac{3}{2} \text { of } x \quad y \text { is } \frac{2}{3} \text { of } x
$$

10 (b) Here is an isosceles trapezium.


Using your answer to part (a).
Write an expression for the perimeter in terms of $x$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

11 The Glasgow Warriors played 15 games of rugby.
Here are the points they scored in each game.

| 8 | 9 | 10 | 20 | 21 | 22 | 23 | 24 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 33 | 34 | 34 | 35 | 43 | 50 |  |

11 (a) Draw a box plot for this information.


Edinburgh Rugby plays against the same 15 teams in the league.

- The median number of points Edinburgh Rugby scored is 18.
- The interquartile range of these points is 14 .
- The range of these points is 31 .

11 (b) Which team is more consistent at scoring points, the
Glasgow Warriors or Edinburgh Rugby?
You must give a reason for your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

12 Here are the interest rates for two accounts.

| Account A |
| :--- |
| Interest: $3 \%$ for the first |
| year |
| $1.5 \%$ for the second year |
| $0.75 \%$ for the third year |
| Withdrawals allowed at any <br> time. |


| Account B |
| :--- |
| Interest: |
| 1.8\% per year compound |
| interest. |
| No withdrawals allowed until <br> the end of three years. |

Headar has $£ 10000$ he wants to invest.

12 (a) Calculate which account would give him the most money if he invests his money for 3 years.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

12 (b) Explain why he might not want to use Account B.
$\qquad$
$\qquad$
$\qquad$

13 It takes 5 men 12 hours to build a wall.
13 (a) How long would it take 8 men to build the wall?
[2 marks]

Answer

13 (b) Comment on an assumption you made in part (a) and the impact this could have on the length of time taken to build the wall.
$\qquad$
$\qquad$
$\qquad$

14 A menu has a choice of 3 starters, 4 mains and 5 desserts. How many different choices of 3 course meals are there? Circle your answer.
12
31
60
120
345

15 The distance by road from Middlesbrough to Buxton is 120 miles.
A brass band travel by coach from Middlesbrough to Buxton.
The coach leaves Middlesbrough at 9:45 am
15 (a) The band assumes the coach will travel at an average speed of 50 mph . Use this assumption to work out the arrival time in Buxton.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

15 (b) In fact, the coach has a higher average speed.
How does this affect the arrival time?
$\qquad$
$\qquad$
$\qquad$

16 Here are two triangles.


Lines PQ and PS are perpendicular to each other.
Work out the length of RS.
Correct to 3 significant figures.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$
$17 A B, C D$, EF are straight lines.
All angles are in degrees.
Not drawn

Show that CD is parallel to EF.


Show that CD is paralel to EF.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


On a Monday morning a speed camera van measured the speed of the cars which passed the van.

There were 20 cars measured as travelling in the range $20 \leq$ speed $<25$.
The speed limit is 30 miles per hour.
Work out the proportion of cars that were caught speeding.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

19


Not drawn accurately

Circle the size of angle ACD.
$99^{\circ}$
$108^{0}$

20 A circle has equation $x^{2}+y^{2}=36$
Circle the length of its diameter.

4
6
12
18
36

21 For all values of $x$,

$$
\begin{aligned}
& f(x)=x^{2}+2 \\
& g(x)=3-x
\end{aligned}
$$

21 (a) Find $f^{-1}(x)$
[2 marks]

## Answer

21 (b) Solve the equation

$$
f g(x)=18
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

22 Here is a Venn diagram representing the universal set, which includes set $A$ and set $B$.

Circle the notation which represent the shaded region.


$$
(A \cap B)^{\prime} \cap A \quad(A \cap B) \cup A \quad A \cap B^{\prime} \quad A \cup B^{\prime}
$$

23 Here is a quadratic sequence.

$$
\begin{array}{llll}
7 & 20 & 39 & 64
\end{array}
$$

The expression for the nth term of this sequence is $p n^{2}+q n$.
Find the value of $p$ and the value of $q$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
p=
$$

$\qquad$

$$
q=
$$

$\qquad$

24 Here is a velocity-time graph for a bike journey.


24 (a) Work out an estimate for the total distance travelled in the first 60 seconds.

25 (a) Show that the equation $x^{3}+5 x=10$ has a solution between $x=1$ and $x=2$.
$\qquad$
$\qquad$
$\qquad$

25 (b) Show that the equation $x^{3}+5 x=10$ can be arranged to give

$$
x=\frac{10}{x^{2}+5}
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$

25 (c) Starting with $x_{0}=1$, use the iteration formula $x_{n}=\frac{10}{x_{n}^{2}+5}$, to find an estimate for the solution of $x^{3}+5 x=10$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

26 A square $A B C D$ is drawn on a centimetre grid.


26 (a) $A B C D$ is reflected in the line $y=4$ and
Circle the number of invariant points.
0
1
2
3
4

26 (b) ABCD is reflected in the line $x=3$ and
then rotated $90^{\circ}$ anti-clockwise from the centre (3,4).
Circle the number of invariant points.

0
1
2
3
4

27 (a) The graph of $y=f(x)$ is shown on the grids.
On this grid, sketch the graph of $y=f(x)-2$

[2 marks]

There are no questions printed on this page

DO NOT WRITE ON THIS PAGE ANSWER IN THE SPACES PROVIDED

